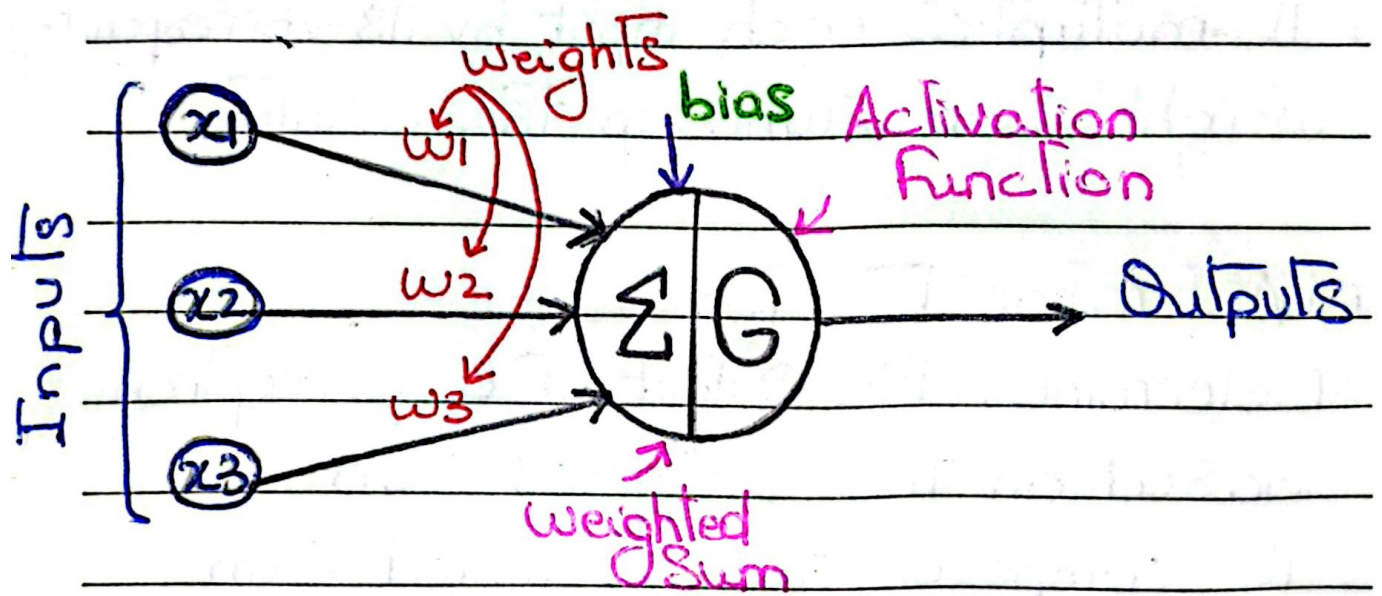


Perceptron

→ What is a Perceptron

- Simplest type of neural network (only have a single neuron)
- Used to classify between linearly separable classes but not complex classification
- Used for binary classification



1) Perceptron Inputs

- Perceptron receives one or more input
- Inputs are called nodes

2) Node Weights

- Values assigned to each input
- Shows the importance of each input
- Higher weight means that the input has a stronger influence of the output

3) Bias

Represents focus on a specific part of the environment

4) Weighted Sum

$\sum \text{weights} \cdot \text{input} + \text{bias}$

The perceptron calculates the weighted sum of its inputs

It multiplies each input by its corresponding weight and sums up the results

5) Activation Function

Determines the output of a perceptron based on the weighted sum

It compares the weighted sum to a threshold value and decide how to trigger the output

In a perceptron we often use "Binary Step" Activation Function

$$y = \text{sign}(\sum w_i x_i + b)$$

$$y = \begin{cases} 1 & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases}$$

There's other types of Activation Functions based on the use case

Steps to train a perceptron

Repeat until convergence (or for a fixed number of iterations)

1. Initialize weights and biases
(assign a random value usually 0)

2. For each training example (x_1, x_2, \dots, x_n) with label y :

• Compute the prediction

$$\hat{y} = \text{Sign}(\sum x_i w_i + b)$$

• if the prediction is incorrect ($\hat{y} \neq y$ or $\hat{y} \cdot y \leq 0$):

→ update each weight: $w_i = w_i + x_i \cdot y$

→ update the bias: $b = b + y$